

الاسم:
الرقم:

مسابقة في مادة الفيزياء
المدة: ساعتان

This exam is formed of three obligatory exercises in 3 pages.
The use of non-programmable calculator is recommended

Exercise 1 (6.5 points)

Determination of the capacitance of a capacitor

The aim of this exercise is to determine the capacitance C of a capacitor. For this aim, consider the electric circuit shown in document 1. The circuit includes a resistor of resistance R , a coil of inductance L and of negligible resistance r , a capacitor of capacitance C , and a low frequency generator (LFG) delivering alternating sinusoidal voltage:

$$u_g = u_{AD} = U_m \cos(\omega t) \quad (u \text{ in V ; } t \text{ in s}).$$

An oscilloscope is connected so as to visualize, as a function of time, the variation of the voltage u_{AD} across the generator on channel Y_1 and the voltage $u_{BD} = u_{\text{coil}}$ across the coil on channel Y_2 (Document 2).

The vertical sensitivity of channel 1 is: $Sv_1 = 5 \text{ V/div}$.

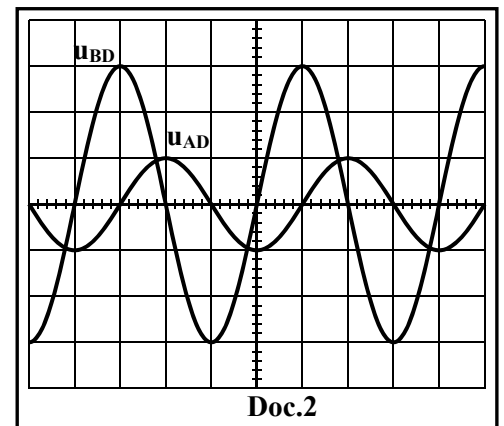
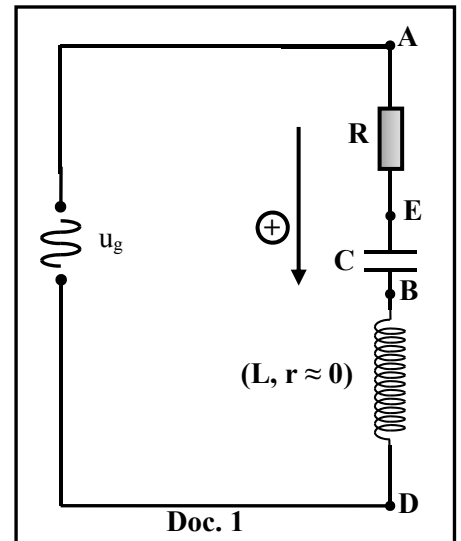
The vertical sensitivity of channel 2 is: $Sv_2 = 2 \text{ V/div}$.

- 1) Redraw the circuit of document 1 showing on it the connections of the oscilloscope.
- 2) Using the waveforms of document 2, determine:
 - 2-1) the amplitudes U_m and $U_{m(\text{coil})}$ of the voltages u_g and u_{coil} .
 - 2-2) the phase difference between the two voltages.
- 3) Write the expression of the voltage u_{coil} across the coil as function of time t and the angular frequency ω .
- 4) The expression of the current i in the circuit is:

$$i = \frac{9.375 \pi}{\omega} \cos(\omega t) \quad (i \text{ in A ; } t \text{ in s}).$$

Determine the expression of the voltage u_{coil} across the terminals of the coil in terms of L , ω and t .

- 5) Using the results of part 3 and 4, show that $L = 0.204 \text{ H}$.
- 6) Indicate the value of the phase difference between u_g and i .
- 7) A phenomenon takes place in the circuit. Name this phenomenon.
- 8) Deduce the value of C knowing that the angular frequency $\omega = 300\pi \text{ rad/s}$.



Exercise 2 (6.5 points)

Ionization and fission of uranium

The aim of this exercise is to study the ionization and the fission of a uranium isotope.

Given:

$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$; speed of light in vacuum: $c = 3 \times 10^8 \text{ m/s}$; Planck's constant: $h = 6.6 \times 10^{-34} \text{ J.s}$.

Mass of $^{235}_{92}\text{U}$ nucleus = 234.99342 u ; $1 \text{ u} = 1.66 \times 10^{-27} \text{ kg}$.

1- Ionizing one of the uranium isotopes

A monochromatic radiation of frequency $\nu = 8 \times 10^{14} \text{ Hz}$ illuminates a sample of uranium containing the isotopes $^{235}_{92}\text{U}$ and $^{238}_{92}\text{U}$.

1-1) Calculate, in Joules and in eV, the energy of a photon of the incident radiation.

1-2) Document 1 shows some of the energy levels of the isotopes $^{235}_{92}\text{U}$ and $^{238}_{92}\text{U}$.

The photons of the incident radiation can excite one of these isotopes of uranium from energy level E_1 to energy level E_2 .

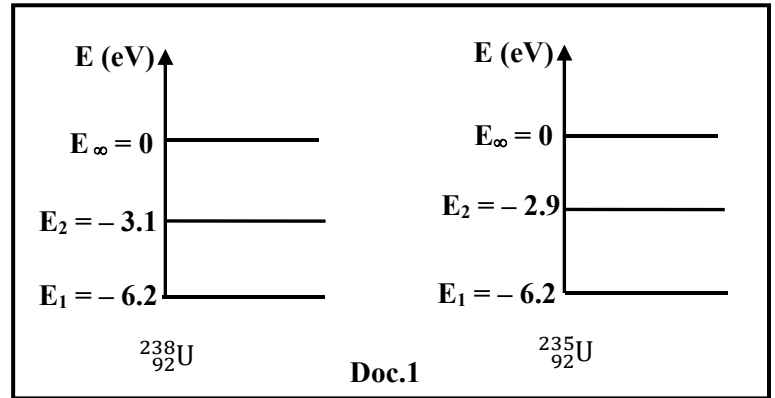
Specify which of the two isotopes will be excited.

1-3) Before it de-excites, the excited isotope receives another photon of same frequency ν .

1-3-1) Show that this isotope will be ionized.

1-3-2) Determine the maximum kinetic energy KE_{max} of the liberated electron.

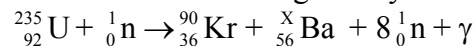
1-4) This experiment shows evidence of one of the two aspects of light. Name this aspect.



2- Nuclear reaction

The isotope of uranium which undergoes fission in the nuclear power plant is uranium-235.

One of the fission reactions of uranium-235 nucleus is given by:



2-1) This reaction is provoked. Why?

2-2) What condition must the projectile satisfy in order to realize this reaction?

2-3) Use one of the conservation laws to calculate x .

2-4) The energy liberated by the fission of each nucleus of uranium-235 is about 200 MeV. In what forms does this energy appear?

2-5) A nuclear power plant of efficiency 40 % furnishes an electric power 600 MW.

Determine, in kg, the mass of uranium-235 consumed in 1 day in this power plant.

Exercise 3 (7 points)

Determination of the mass of a block and the stiffness of a spring

Consider two blocks, (A) of unknown mass m_A and (B) of mass $m_B = 0.8 \text{ kg}$, and a spring (R) of negligible mass and of stiffness k . The aim of this exercise is to determine m_A and k .

Neglect all the forces of friction and take $g = 10 \text{ m/s}^2$.

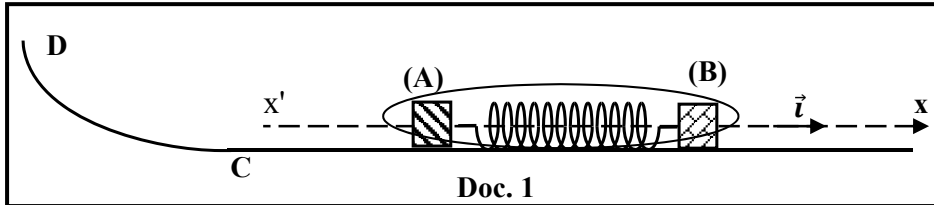
1- First experiment: Determination of m_A

The spring is placed on a horizontal track. The spring is compressed between (A) and (B) by means of a light string (Document 1).

The center of mass of (A) and that of (B) belong to the same horizontal plane which is taken as a reference level for gravitational potential energy.

The x-axis extends positively to the right.

We burn the string, (A) and (B) are ejected in opposite directions.



1-1) Name the external forces acting on the system [(A), (B) and (R)].

1-2) Deduce that the linear momentum of the system [(A), (B) and (R)] is conserved during the motion of (A) and (B) on the horizontal track.

1-3) The velocity of the center of mass of block (B) just after ejection is $\vec{V}_B = 0.75 \vec{i}$ (m/s).

1-3-1) Determine the linear momentum \vec{P}_A of block (A).

1-3-2) Deduce in terms of m_A the velocity \vec{V}_A of the center of mass of (A) just after ejection.

1-4) Block (A) continues its motion and reaches a curvilinear path CD situated in the vertical plane (Document 1). The maximum height attained by the center of mass of (A) above the reference level is $h_{\max} = 5$ cm.

1-4-1) Apply the principle of conservation of mechanical energy to the system [(A), Earth] to determine the magnitude V_A of \vec{V}_A .

1-4-2) Deduce the value of the mass m_A .

2- Second experiment: Determination of k

We fix block (B) to one of the ends of the spring (R), the other end of the spring is attached to a fixed support (Document 2).

At equilibrium, (B) is at O taken as an origin of abscissa of the axis x'x.

(B) is displaced, from point O along the axis x'x by a distance X_m in the negative direction, and then it is released without initial velocity at the instant $t_0 = 0$. At an instant t, the abscissa of the center of mass G of (B) is x and the algebraic measure of its velocity is v.

During the motion of (B) between $t_0 = 0$ and $t = \frac{T_0}{2}$ [T_0 is the proper period of the oscillations of (B)], an appropriate system traces the graphs of documents (3) and (4).

Document (3): represents the variation of the speed of G as a function of time.

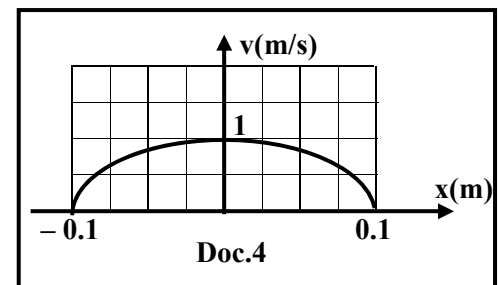
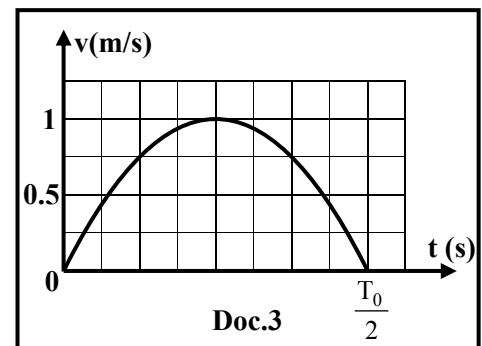
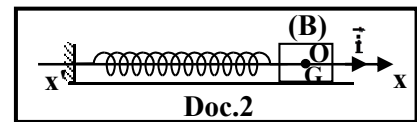
Document (4): represents the variation of the speed of G as a function of the abscissa x.

2-1) Determine, by referring to document (3), the value of the maximum kinetic energy of (B).

2-2) Deduce the value of the maximum elastic potential energy of the system [(R), (B), Earth].

2-3) Indicate, by referring to document (4), the value of X_m .

2-4) Deduce the value of k.



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Exercise 1 : Determination the capacitance of a capacitor			
Question	Answer	mark	
1		0.5	
2	2-1	$U_{\max(g)} = y \times Sv_1 = 5V$ $U_{\max(l)} = y \times Sv_2 = 6V$	0.5 0.5
	2-2	$\Delta\phi = \frac{2\pi d}{D} = \frac{\pi}{2} \text{ rad.}$	0.5
3	$u_{\text{coil}} = 6 \cos(\omega t + \frac{\pi}{2}) = -6 \sin(\omega t)$	0.75	
4	$u_{\text{coil}} = L \frac{di}{dt} = -L \times 9.375 \pi \sin(\omega t).$	1	
5	$u_{\text{coil}} = u_{\text{coil}}, \text{ then } 6 = L \times 9.375 \pi ; \text{ then } L = 0.204 \text{ H.}$	1	
6	zero	0.5	
7	Current resonance	0.5	
8	Current resonance, $LC(\omega)^2 = 1, C = 5.518 \mu F.$	0.75	

Exercise 2 : Ionization and fission of uranium

Question		Answer	mark
1	1	$E = h\nu$	0.25
		$E = 6.6 \times 10^{-34} \times 8 \times 10^{14} = 5.28 \times 10^{-19} \text{J}$	0.5
		$E = 3.3 \text{ eV}$	0.25
	2	$E = 3,3 \text{ eV} = E_2 - E_1$ for ${}^{235}_{92}\text{U}$	0.5
		${}^{235}_{92}\text{U}$ can be excited	0.25
3	1	$E_{\text{ionisation}} = E_{\infty} - E_2 = 2,9\text{eV}$ $E_{\text{photon}} > 2.9 \text{ eV}$, the isotope can be ionized	0.25 0.5
	2	$E_{\text{photon}} = (E_{\infty} - E_2) + K.E_{\text{max}} = E_{\text{ionisation}} + K.E_{\text{max}}$ $K.E_{\text{max}} = 0.4 \text{ eV}$	0.5 0.5
4	Aspect corpuscular of light		0.25
2	1	Since it has an external intervention (bombarded by a neutron)	0.25
	2	Thermal neutron or slow neutron or $KE \approx 0.025 \text{ eV}$	0.25
	3	Law of conservation of mass number: $x = 138$	0.5
	4	Kinetic energy of emitted nuclei, KE of emitted particles, energy of photons γ	0.5
	5	$E_{\text{elect}} = P \times t = 600 \times 10^6 \times 24 \times 3600 = 5.184 \times 10^{13} \text{J}$ efficiency = $\frac{E_{\text{electrique}}}{E_{\text{nucléaire}}}$; $E_{\text{nuclear}} = E_{\text{elect}} \frac{100}{40} = 1.296 \times 10^{14} \text{J}$ $m({}^{235}_{92}\text{U}) = 234.99342 \text{ u} = 234.99342 \times 1,66 \times 10^{-27} \text{ kg} = 3.90 \times 10^{-25} \text{ kg}$ $200 \text{ MeV} = 200 \times 1,6 \times 10^{-13} \text{ J} = 3.20 \times 10^{-11} \text{J}$ $m_{\text{totale}} = \frac{1.296 \times 10^{14} \times 3.90 \times 10^{-25}}{3.20 \times 10^{-11}} = 1.58 \text{ kg}$	1.25

Exercise 3 : Determination of the mass of a block and the stiffness of a spring				
Question	Answer	Mark		
1	1-1	Weight $m_A \vec{g}$ of (A), normal reaction \vec{N}_A on (A), Weight $m_B \vec{g}$ de (B), normal reaction \vec{N}_B on (B).	0.5	
	1-2	$\Sigma \vec{F}_{\text{ext}} = \frac{d\vec{P}}{dt}$, then $m_A \vec{g} + \vec{N}_A + m_B \vec{g} + \vec{N}_B = \vec{0} = \frac{d\vec{P}}{dt}$, The linear momentum of the system (A, B, spring) is conserved.	0.75	
	3	1	$\vec{P}_{\text{initial}} = \vec{P}_{\text{final}}$, then $\vec{0} = \vec{P}_A + \vec{P}_B$, $\vec{P}_A = -\vec{P}_B$ $\vec{P}_A = -m_B \vec{V}_B = -0.8 \times 0.75 \vec{i} = -0.6 \vec{i}$ (kg.m/s)	1
		2	$\vec{P}_A = m_A \vec{V}_A$, $\vec{V}_A = -\frac{0.6}{m_A} \vec{i}$ (m/s).	0.5
	4	1	Let F the maximum point reached by (A) $ME_1 = ME_2$, $\frac{1}{2} m_A V_A^2 + m_A g h_A = \frac{1}{2} m_A V_F^2 + m_A g h_{\text{max}}$ $\frac{1}{2} m_A V_A^2 = m_A g h_{\text{max}}$, $V_A = \sqrt{2 \times g \times h_{\text{max}}} = \sqrt{2 \times 10 \times 0.05} = 1$ m/s	1.25
		2	$V_A = \frac{0.6}{m_A} = 1$, then $m_A = 0.6$ kg.	0.5
2	2-1	Graphically $V_{\text{max}} = 1$ m/s $KE_{\text{max}} = \frac{1}{2} m_B V_{\text{max}}^2 = 0.4$ J	0.75	
	2-2	The mechanical energy of the system is conserved: $PE_{\text{max}} = KE_{\text{max}} = 0.4$ J	0.5	
	2-3	$X_{\text{max}} = 10$ cm	0.5	
	2-4	$\frac{1}{2} k X_{\text{max}}^2 = 0.4$ then $k = 80$ N/m	0.75	

